

# A Threshold Signature Protocol Implementation via JavaCard API



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Centre for Research on  
Cryptography and Security

# Outline

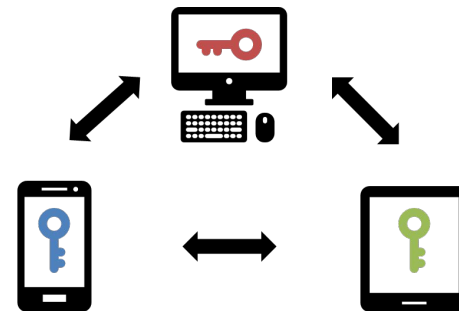
- Introduction
- Threshold signatures
  - Secure secret sharing
  - Threshold protocols
- Problems in use of threshold signatures
- JCFROST implementation
  - FROST protocol
  - JavaCard smartcards
  - Performance measurements
  - Demonstration
- Conclusion

# Threshold signatures

- A concept mainly developed 90's is now starting to be used in modern applications
  - Cryptocurrencies (multi-signature wallets)
  - Authentication (eIDAS-compliant – SplitKey/SmartID)



Single party computation



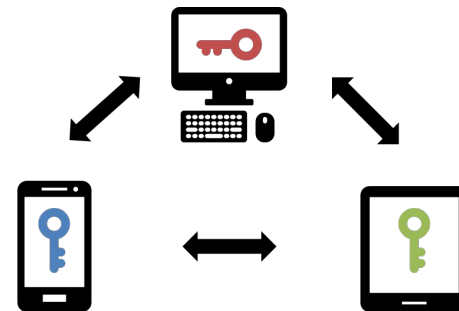
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# Threshold signatures

- A concept mainly developed 90's is now starting to be used in modern applications
  - Cryptocurrencies (multi-signature wallets)
  - Authentication (eIDAS-compliant – SplitKey/SmartID)
- A convenient private key protection method
  - Decentralization of storage
  - Elimination of single point of failure
  - Easy integration with existing systems (backward compatibility)



Single party computation



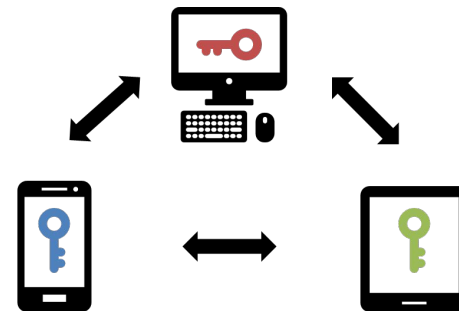
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# Secure secret sharing

- Splitting a secret into  $n$  shares
  - At least  $t$  shares are needed to reconstruct the secret
  - Less than  $t$  shares gives *no information* about the secret
  - Can be created “bottom-up” using distributed key generation



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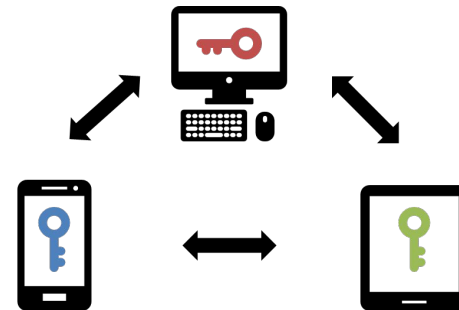
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- Additive secret sharing ( $n$ -of- $n$ )
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  - Supports non-interactive key generation



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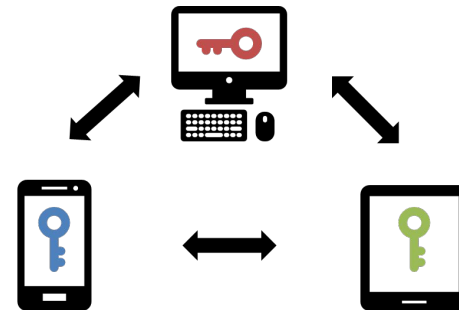
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- Shamir’s secret sharing ( $t$ -of- $n$ )
  - Only  $t$  shares are needed to reconstruct the secret



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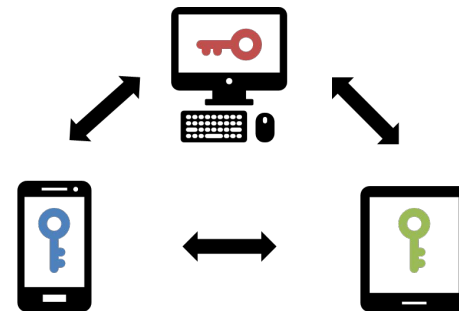
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- Devices operate with secret shares directly
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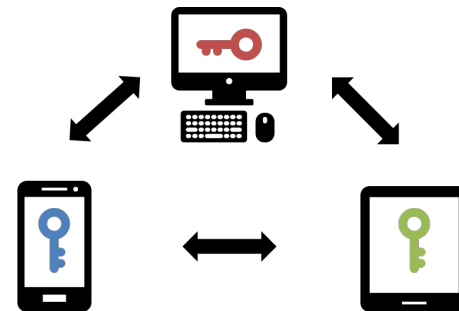


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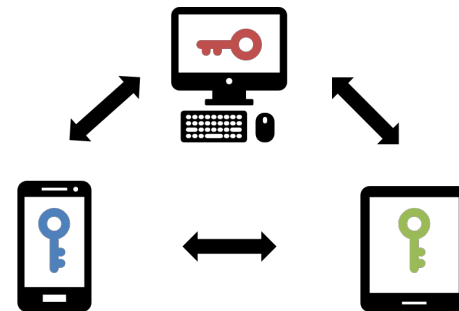
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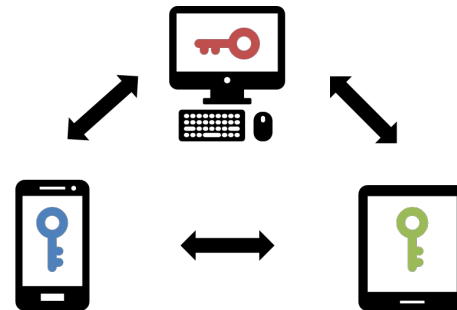
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- Typically require
  - Multiple communication rounds
  - More complex computation compared to the base operation



Single party computation



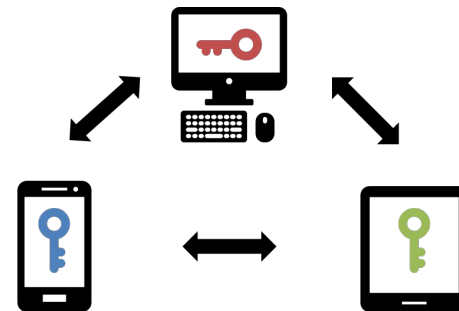
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- Protocol selection
  - Several protocols exist for each signature type
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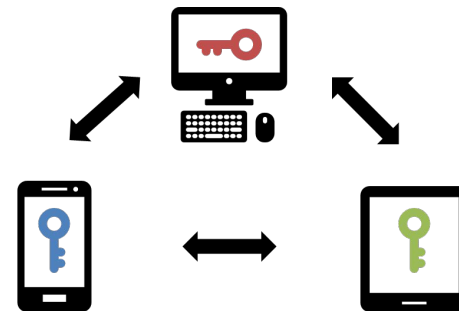
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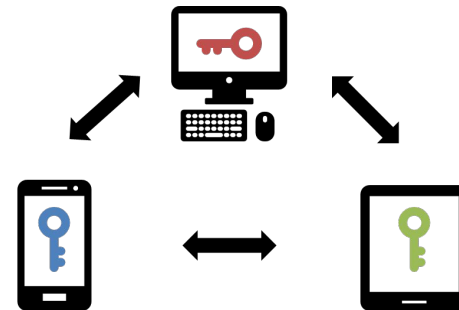
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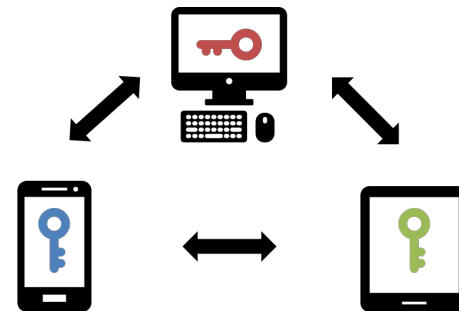
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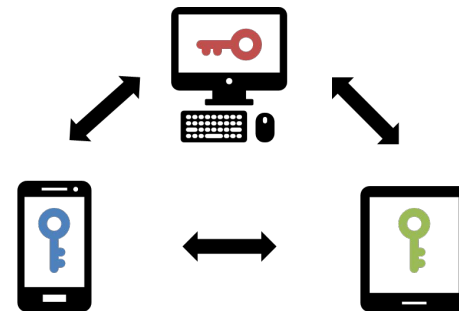
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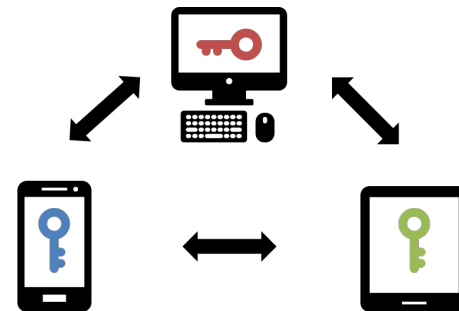


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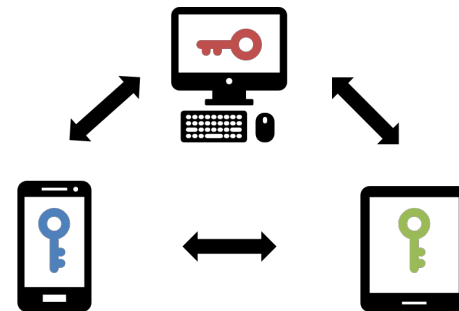
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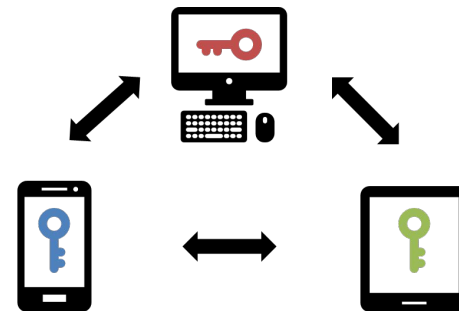
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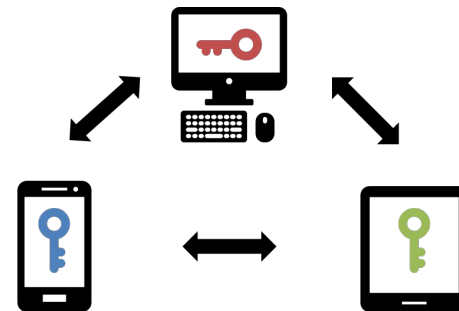
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  - But they do not support threshold protocols
- Threshold protocols are not standardized
- Secure hardware may not be able to run the protocols
  - Hardware constraints
  - Limited interface and programmability



Single party computation



Threshold computation

## Research question

Can state-of-the-art threshold protocols be computed efficiently on current secure hardware?

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- Two communication rounds
  - The first is offline (precomputable)
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- The computation requires
  - Modular arithmetic (addition, subtraction, multiplication, inversion)
  - Elliptic curves (point addition, scalar multiplication)
  - Hash function

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- Generic CPU
  - Programmable with Java-like code that gets executed in JCVM
  - Insufficient performance for current public-key cryptography
- Hardware accelerators
  - Accessible only via high-level JC API algorithms (RSA, DH, ECDH, ...)
  - Lack of low-level operation access (addition, multiplication, EC addition)
  - Repurposing algorithms to perform low-level operations



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- We extended the library
  - Support for new cards
  - Faster operations on new cards
    - Modular multiplication (4.5x speedup)
    - Accelerated point addition (7x speedup)
    - Fully accelerated scalar multiplication (4x speedup)
  - Added new operations
    - Combined point addition and multiplication (useful for FROST)
    - Point encoding and decoding

# FROST on JavaCards

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- Open-source FROST protocol implementation for JavaCards
  - Implements FROST(secp256k1, SHA-256)
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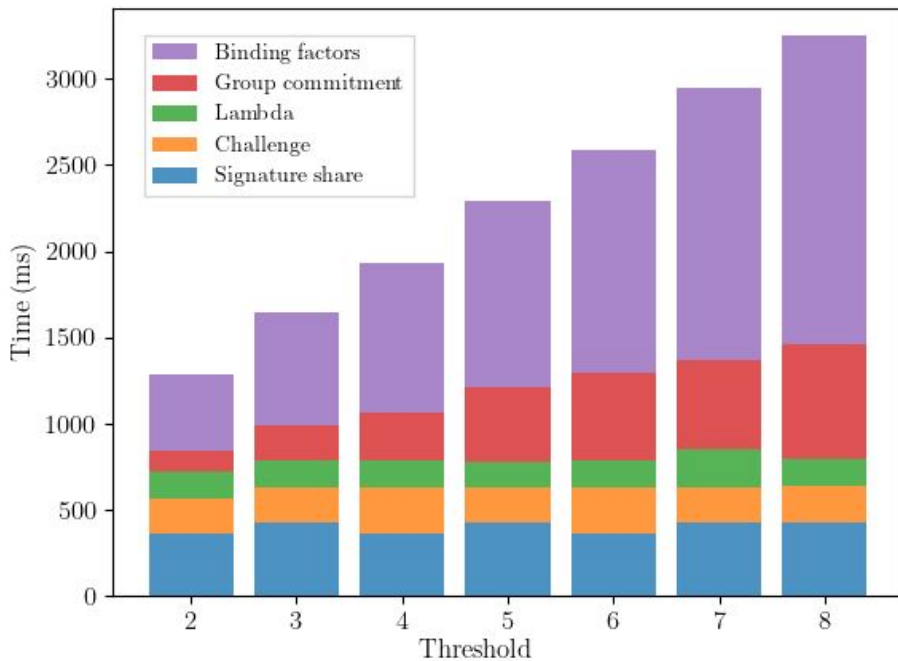
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  - Constrained lambda computation ( $n \leq 12$  or  $n \leq 7$ )
    - Intermediate computations can fit in int or short (depending on the constraint)
    - Allows for significant performance improvement over BigInteger-based version

# Performance results

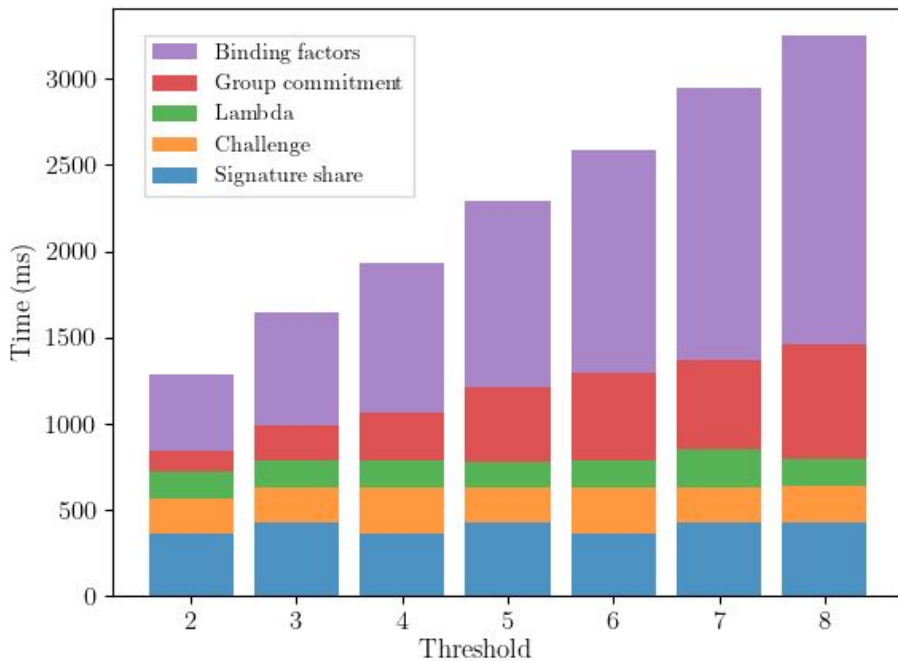


## NXP J3R200 (2020)

- $t < 5$  can be computed under 2s



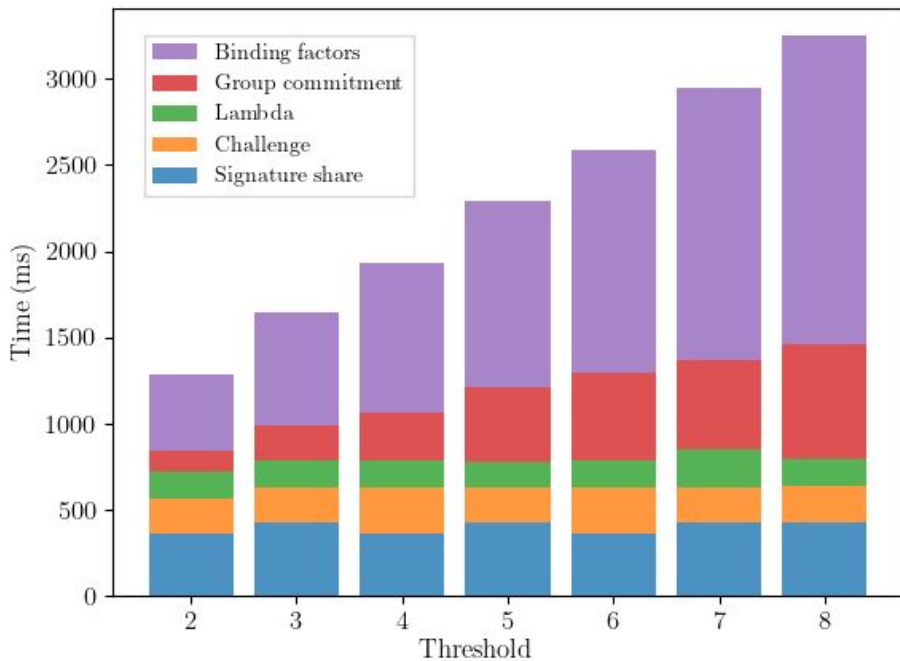
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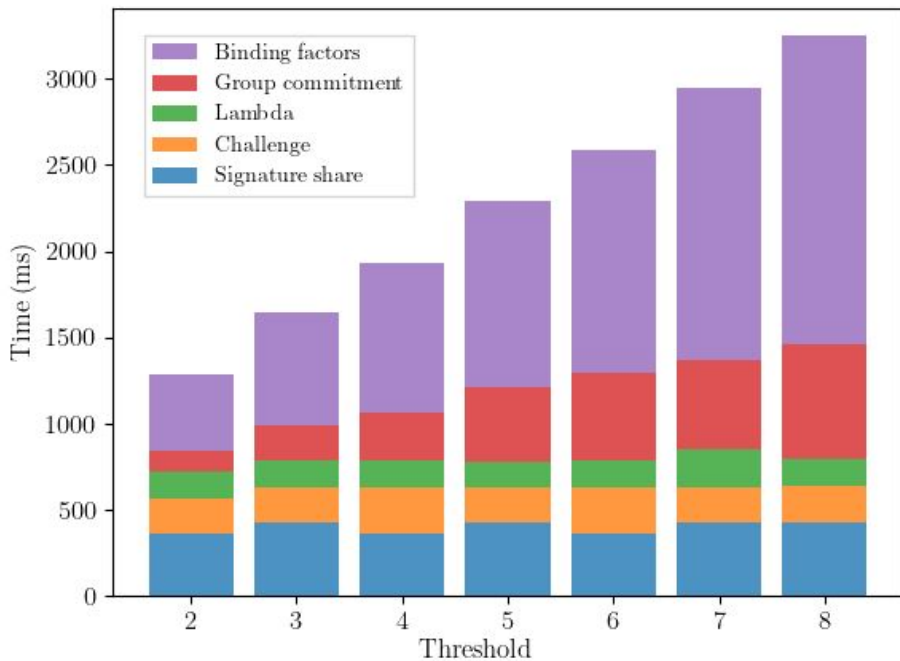
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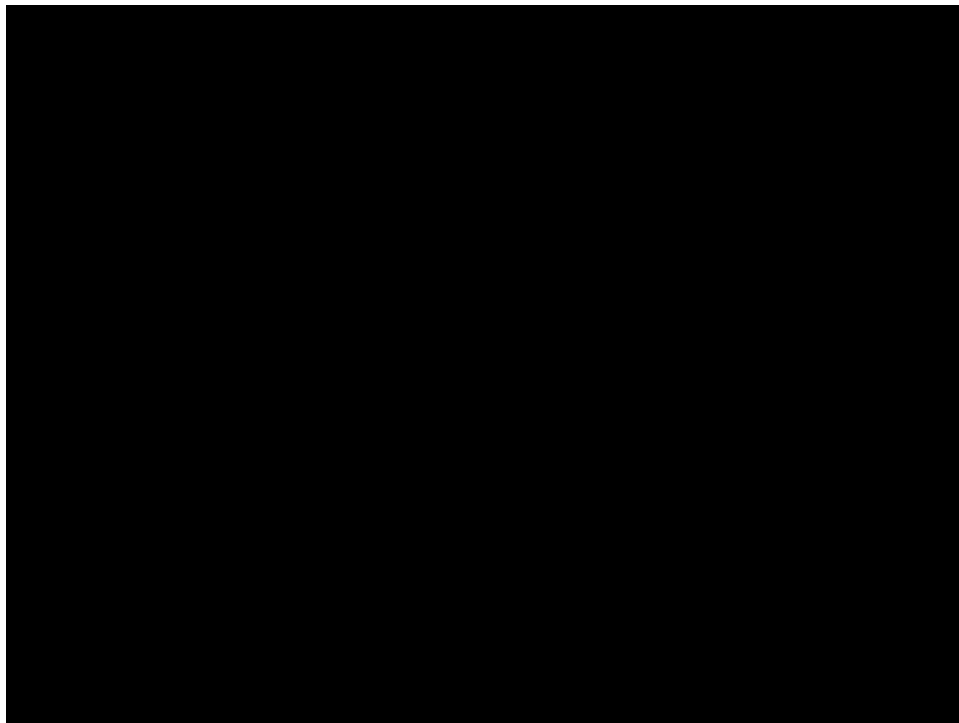
# Performance results



## NXP J3R200 (2020)

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- Linear growth with threshold
- **Group commitment** performs on the platform's limits
- Other operations could be notably faster with low-level access to the platform

# Demonstration



## Conclusion

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- Can threshold protocol FROST be computed efficiently on current JavaCards?
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  - Performance improvements possible using proprietary low-level interface
- The positive result can generalize to similar EC-based schemes
  - CoSi [Syt+17], MuSig2 [JRS21], SimpleTSig [CKM22], Lindell22 [Lin22]
- On the contrary
  - ECDSA-based protocols currently seem too complex for this approach
  - Post-quantum signatures are mostly too demanding even in the single-party case

# Thank you for your attention

JCFROST implementation



<https://github.com/crocs-muni/JCFROST>

JCMathLib library



<https://github.com/OpenCryptoProject/JCMathLib>



## References

- [KG21] Komlo, Chelsea, and Ian Goldberg. "FROST: flexible round-optimized Schnorr threshold signatures." Selected Areas in Cryptography: 27th International Conference, Halifax, NS, Canada (Virtual Event), October 21-23, 2020, Revised Selected Papers 27. Springer International Publishing, 2021.
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